

Decadal Prediction Drift as a Particular Challenge for Verification

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7th Int. Verification Methods Workshop, Berlin, May 11th, 2017

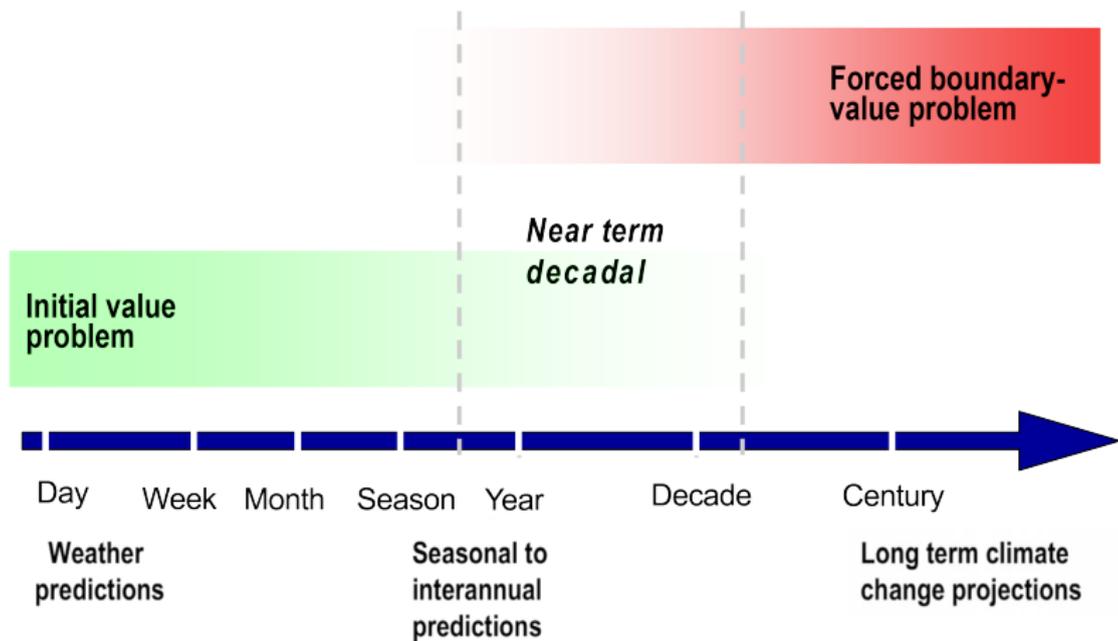
Decadal climate prediction . . .

*. . . provides information about the future evolution of the statistics of regional climate from the output of a numerical model that has been **initialized with observations** . . .*

1

¹cited from Meehl et al. [2014]

Decadal climate prediction ...

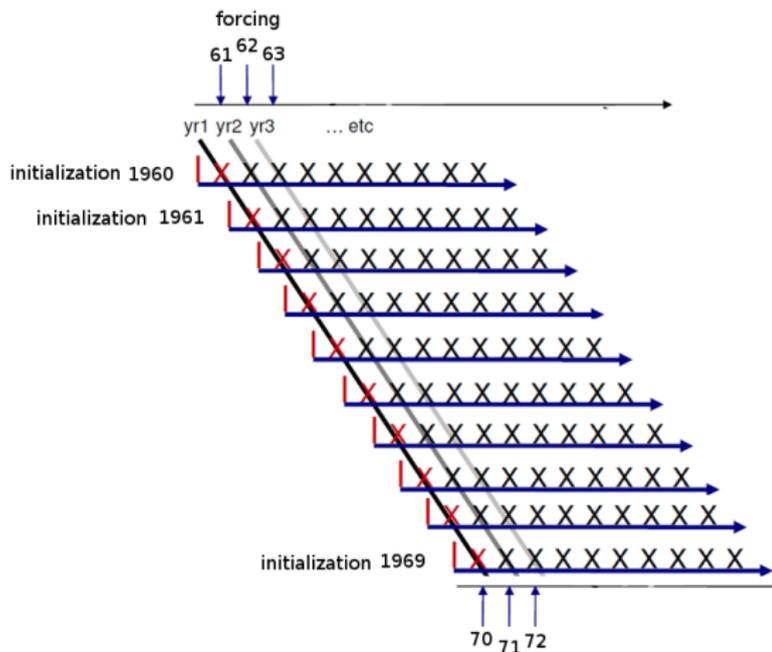


2

²taken from Boer et al. [2016]

Initialization with “observations”

Hindcast set: initialize every year, 10-yr hindcast each



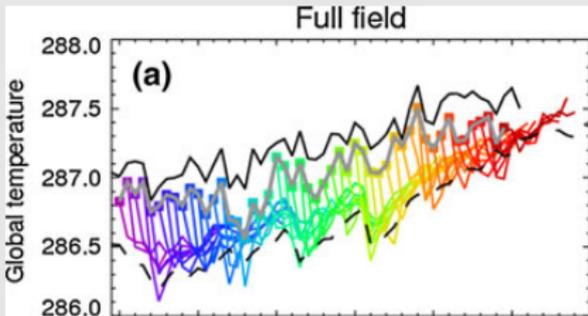
courtesy of Jens Grieger

Initialization with “observations”

Hindcast set: initialize every year, 10-yr hindcast each

Full-field

assimilate directly



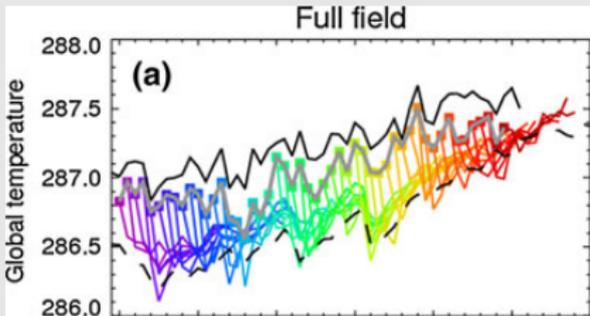
Annual mean global temperature,
taken from [Smith et al. \[2013\]](#)

Initialization with “observations”

Hindcast set: initialize every year, 10-yr hindcast each

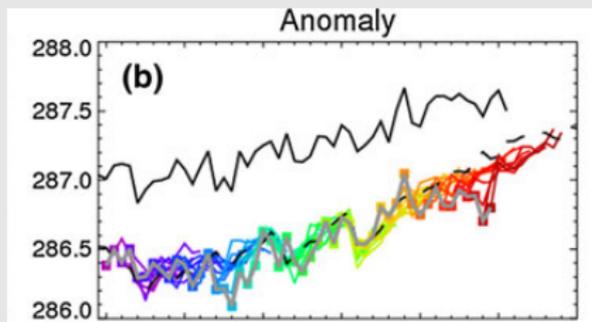
Full-field

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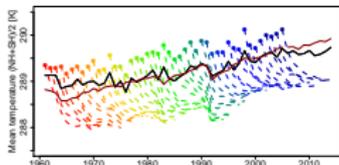
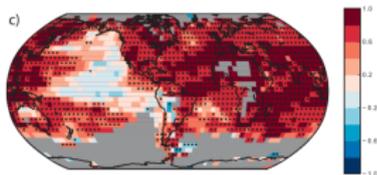
Anomaly

assimilate anomalies

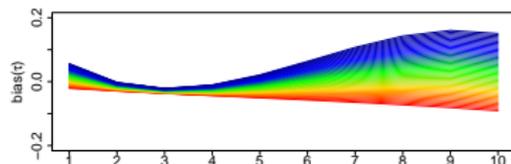


Annual mean global temperature,
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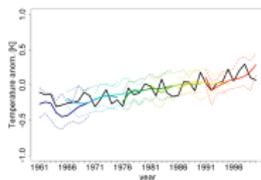
Verification of decadal prediction



Drift



Drift adjustment



Re-Calibration

A framework

Clim Dyn (2013) 40:245–272
DOI 10.1007/s00382-012-1481-2

A verification framework for interannual-to-decadal predictions experiments

L. Goddard · A. Kumar · A. Solomon · D. Smith · G. Boer · P. Gonzalez · V. Kharin · W. Merryfield · C. Deser · S. J. Mason · B. P. Kirtman · R. Msadek · R. Sutton · E. Hawkins · T. Fricker · G. Hegerl · C. A. T. Ferro · D. B. Stephenson · G. A. Meehl · T. Stockdale · R. Burgman · A. M. Greene · Y. Kushnir · M. Newman · J. Carton · I. Fukumori · T. Delworth

Received: 10 October 2011 / Accepted: 31 July 2012 / Published online: 24 August 2012
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Received: 10 October 2011 / Accepted: 31 July 2012 / Published online: 24 August 2012
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Q1: Predictions more accurate due to initialization?

Q2: Does ensemble spread appropriately represents uncertainty?

Verification: What can we expect?³

Temporal scales

annual/seasonal averages

1yr lead-year 1

4yrs lead-years 2-5, 6-9

8yrs lead-years 2-9

more are preferable

³Decadal prediction verification framework [Goddard et al. \[2013\]](#)

Verification: What can we expect?³

Temporal scales	Spatial scales
annual/seasonal averages	scale of reference or larger, e.g.
1yr lead-year 1	Temp 5°×5°
4yrs lead-years 2-5, 6-9	Precip 2.5°×2.5°
8yrs lead-years 2-9	depends on study
more are preferable	

³Decadal prediction verification framework [Goddard et al. \[2013\]](#)

Verifying ensemble predictions: Accuracy of mean

Ensemble mean

$$H_{j\tau} = \frac{1}{N_e} \sum_{i=1}^{N_e} H_{ij\tau}$$

$H_{ij\tau}$ ens. member i , initialization j , lead-year τ

Verifying ensemble predictions: Accuracy of mean

Ensemble mean

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$H_{ij\tau}$ ens. member i , initialization j , lead-year τ

Q1: More accurate due to initialization?

$$MSESS = 1 - \frac{MSE_H}{MSE_R}$$

historicals (no initialization but forcing) as reference

Verifying ensemble predictions: Spread

Ensemble Spread

$$\sigma_{H_j}^2 = \frac{1}{N_e - 1} \sum_{i=1}^{N_e} (H_{ij\tau} - H_{j\tau})^2$$

Verifying ensemble predictions: Spread

Ensemble Spread

$$\sigma_{H_j}^2 = \frac{1}{N_e - 1} \sum_{i=1}^{N_e} (H_{ij\tau} - H_{j\tau})^2$$

Q2: Does ensemble spread appropriately represents uncertainty?

$$CRPS(\mathcal{N}(\hat{H}_j, \overline{\sigma^2_H}), O_j)$$

Gaussian hindcast distribution^a
conditional and unconditional bias adjusted (\hat{H}_j)

^aGneiting and Raftery [2007]

Verifying ensemble predictions: Spread

Ensemble Spread

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MSE as variance of ref. forecast, CRPSS=0 is optimal!

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Q2: Does ensemble spread appropriately represents uncertainty?

$$CRPSS = 1 - \frac{\overline{CRPS_H}}{\overline{CRPS_R}}$$

MSE as variance of ref. forecast, CRPSS=0 is optimal!

$$LESS = \ln \left(\frac{\overline{\sigma_H^2}}{\overline{MSE}} \right)$$

Additionally, logarithmic ensemble spread score
e.g. [Kadow et al. \[2014\]](#)

Small ensembles and significance

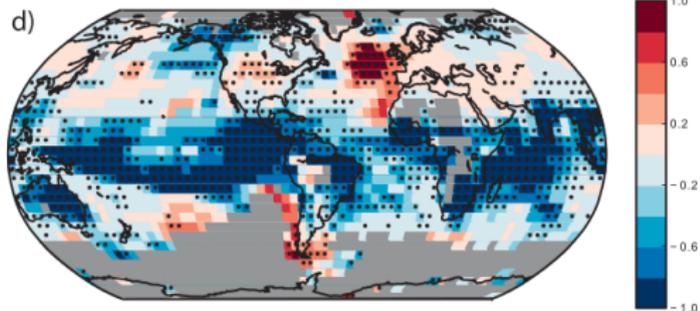
MiKlip ensembles

baseline0 3

baseline1 10

prototype 15 + 15

preop ≤ 15



Goddard et al. [2013] suggest a bootstrap for significance

Small ensembles and significance

MiKlip ensembles

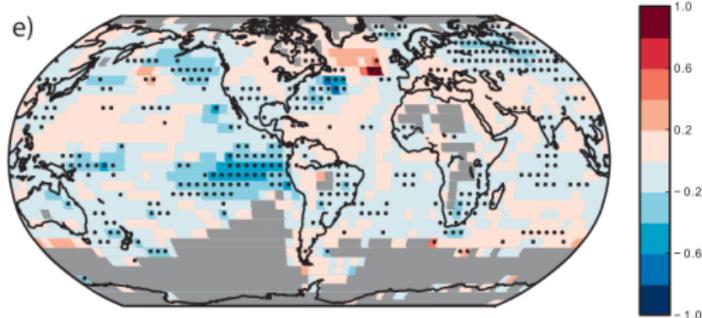
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Small ensembles and significance

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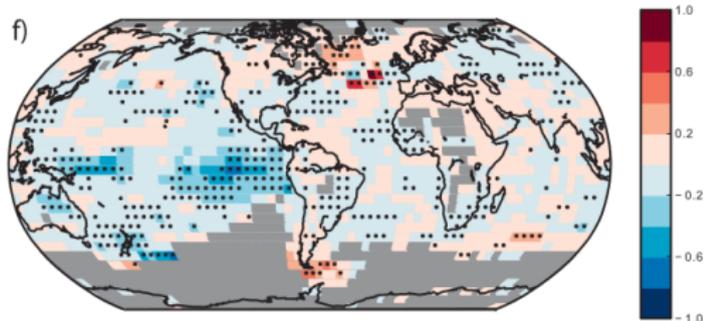
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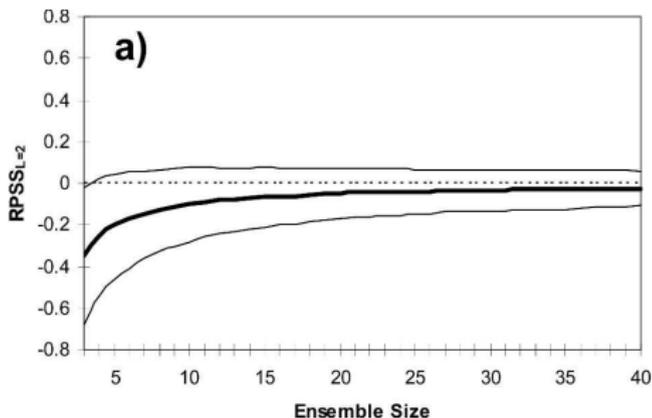
preop ≤ 15

f)



Goddard et al. [2013] suggest a bootstrap for significance

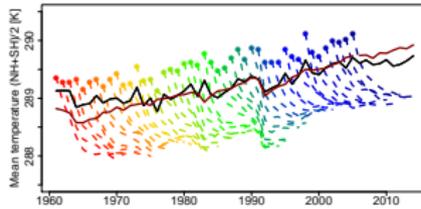
Small ensembles and biased scores



4

- bias corrected scores [Ferro et al. \[2008\]](#)
- application with RPS [Kruschke et al. \[2015\]](#)
- implemented in R-package `SpecsVerification` (Stefan Siegert)

⁴taken from [Müller et al. \[2005\]](#)



Drift

“Bias” or mean difference

$$ME = \frac{1}{N} \sum_{j=1}^N H_j - \frac{1}{N} \sum_{j=1}^N O_j$$

“Bias” or mean difference

$$ME = \frac{1}{N} \sum_{j=1}^N H_j - \frac{1}{N} \sum_{j=1}^N O_j := b$$

For decadal prediction and other cases

$$b = b(\tau, \mathbf{X}),$$

τ : forecast lead-time; \mathbf{X} and climate state \mathbf{X} .

Systematic error we believe we can compensate *a posteriori*

Drift

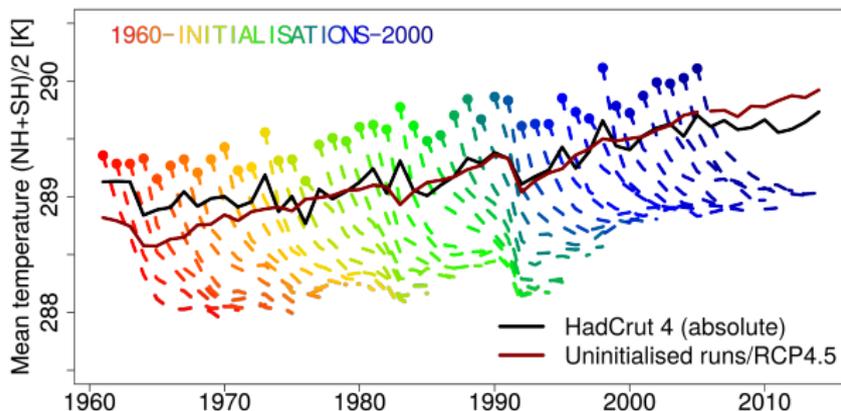
change in bias with forecast lead-time τ

$$D(\tau, \mathbf{X}) = \frac{\partial}{\partial \tau} b(\tau, \mathbf{X})$$

Drift

change in bias with forecast lead-time τ

$$D(\tau, \mathbf{X}) = \frac{\partial}{\partial \tau} b(\tau, \mathbf{X})$$

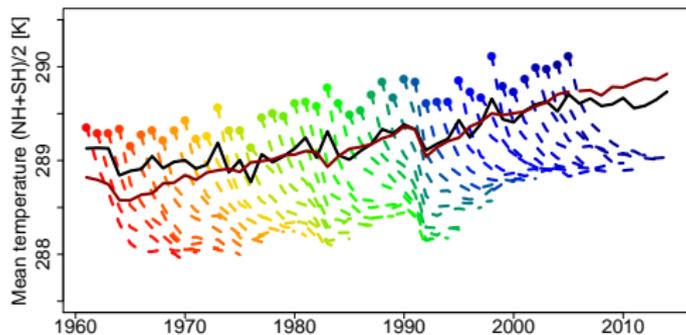


Quantifying drift

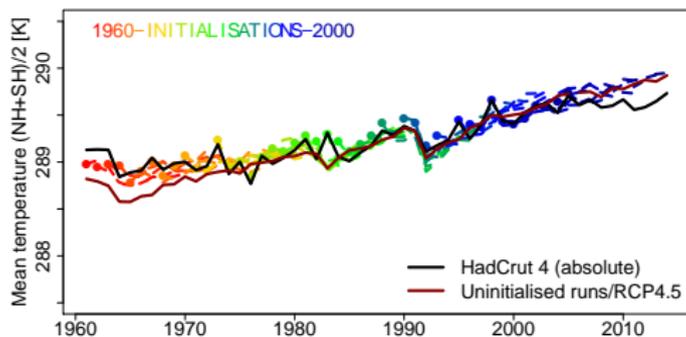
$$\begin{aligned}\|D(\tau, \mathbf{X})\| &= \sqrt{(D(\tau, \mathbf{X}))^2} \\ &= \sqrt{\left(\frac{\partial}{\partial \tau} b(\tau, \mathbf{X})\right)^2}\end{aligned}$$

Igor Kröner *Drift Quantification and Correction in Decadal Predictions of Climate Extremes Indices*, in preparation

Examples from MiKlip: Drift in global mean temperature



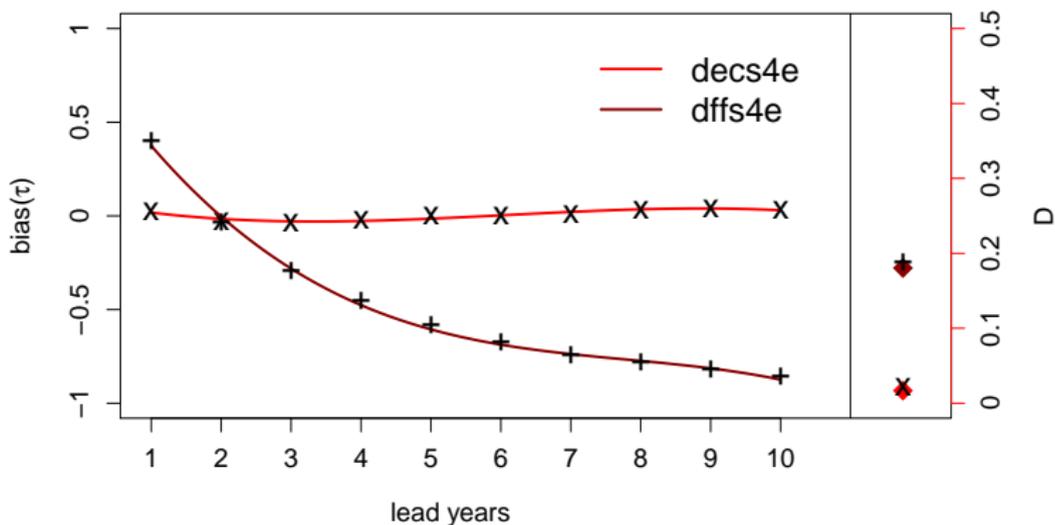
full-field



anomaly

courtesy of Igor Kröner

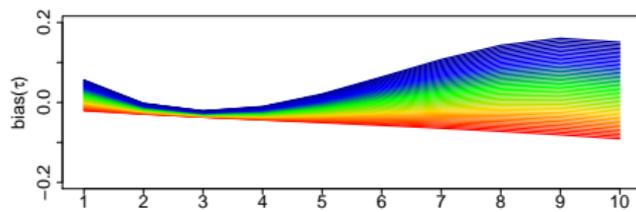
Examples from MiKlip: Drift in global mean temperature



red anomaly initialisation (baseline1, decs4e)

brown full-field initialisation (prototype, dffs4e)

courtesy of Igor Kröner



Drift Adjustment

Verification of forecasts with bias/drift

$$S(H(t, \tau), o(t))$$

Verification of forecasts with bias/drift

$$S(H(t, \tau), o(t))$$

How good is the forecast once we have compensated for systematic errors?

Verification of forecasts with bias/drift

$$S(\hat{H}(t, \tau), o(t))$$

$$\hat{H}(t, \tau) = H(t, \tau) - \hat{b}(t, \tau)$$

Verification of forecasts with bias/drift

$$S(\hat{H}(t, \tau), o(t))$$

$$\hat{H}(t, \tau) = H(t, \tau) - \hat{b}(t, \tau)$$

Recommendation^a full-field and anomalies

assume $b(\tau, \mathbf{X}(t)) = b(\tau, t)$

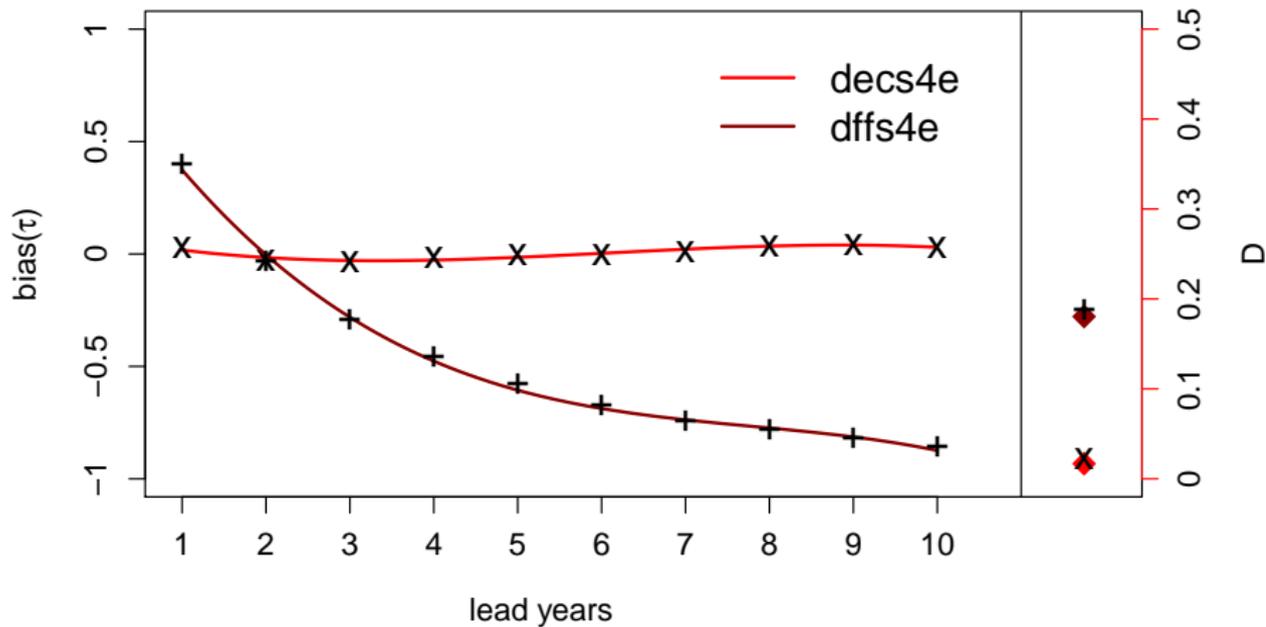
$$\hat{b}_{ICPO}(t, \tau) = \frac{1}{\#\{t_i \setminus t\}} \sum_{t_i \setminus t} (H(t_i, \tau) - o(t_i)) \approx ME(\tau)$$

yr of forecast to be verified left out (ICPO 2011)

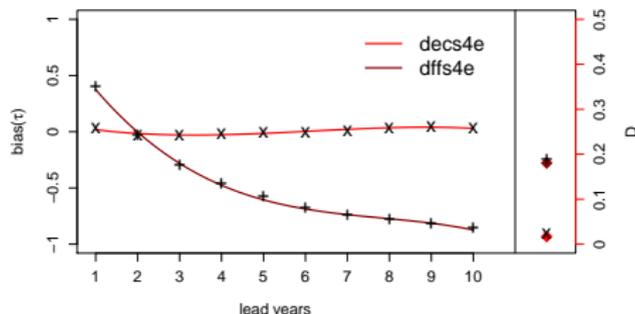
lead-years τ are treated individually

^aBoer et al. [2016]

Back to the drift ...



Back to the drift ...



Drift ist smooth in τ

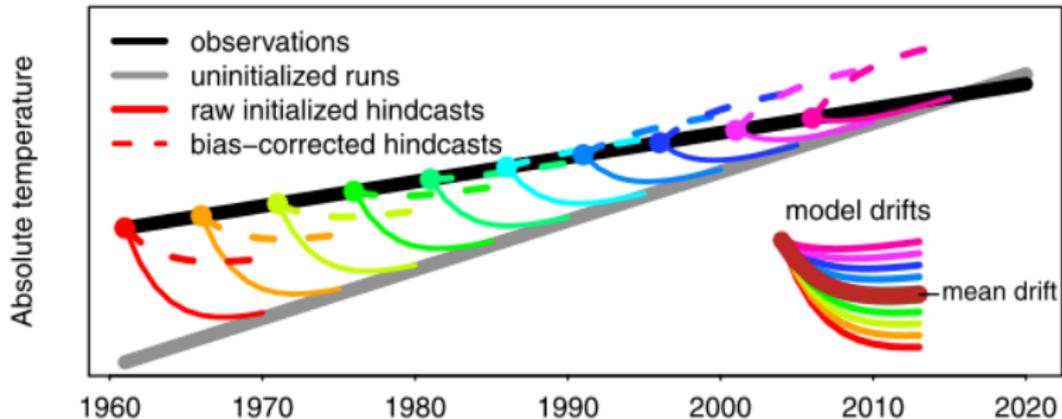
$b(\tau, \mathbf{X}(t)) = b(\tau)$, smooth/parametric form in τ

$$\hat{b}_{Gan}(t, \tau) = a_0 + a_1 \tau + a_2 \tau^2 + a_3 \tau^3$$

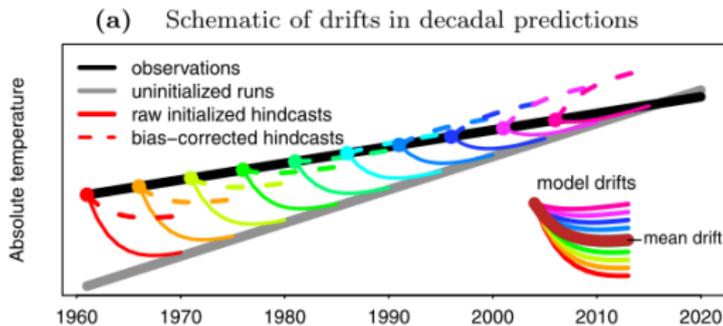
third order polynomial in τ Gangstø et al. [2013]
(exponential Pattantyús-Ábrahám et al. [2016])

Back to the drift ...

(a) Schematic of drifts in decadal predictions



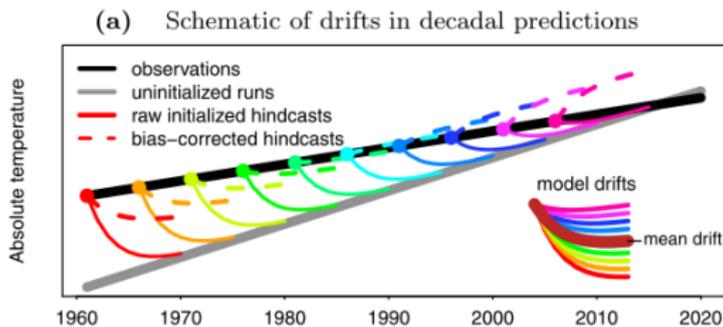
Back to the drift . . .



Drift might change with climate (t)⁵

⁵Kharin et al. [2012]Fučkar et al. [2014]

Back to the drift ...

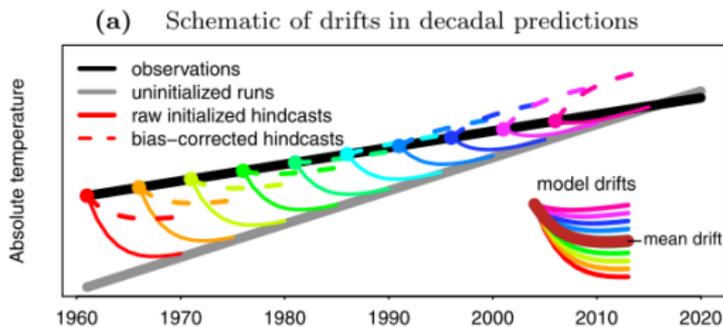


Drift might change with climate (t)⁵

$$\hat{b}(t, \tau) = a_0 + a_1 \tau + a_2 \tau^2 + a_3 \tau^3$$

⁵Kharin et al. [2012]Fučkar et al. [2014]

Back to the drift ...

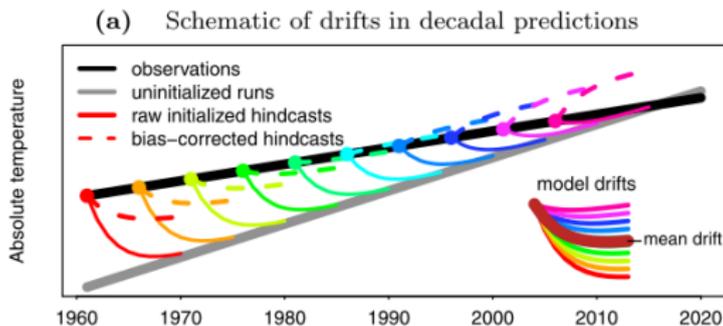


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Back to the drift ...



Drift might change with climate (t)⁵

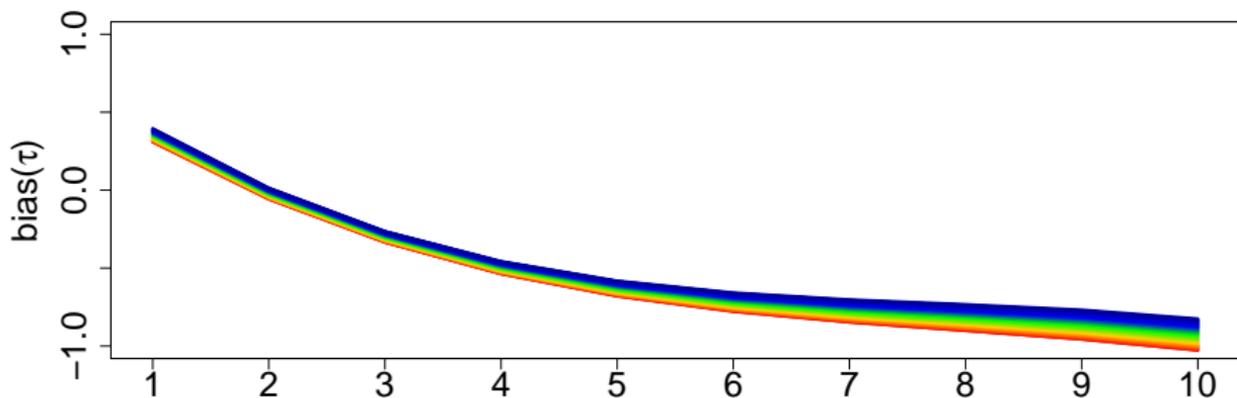
$$\hat{b}_{Kru}(t, \tau) = (b_0 + b_1 t) + (b_2 + b_3 t) \tau + (b_4 + b_5 t) \tau^2 + (b_6 + b_7 t) \tau^3$$

Kruschke et al. [2015]

⁵Kharin et al. [2012]Fučkar et al. [2014]

Drift ...

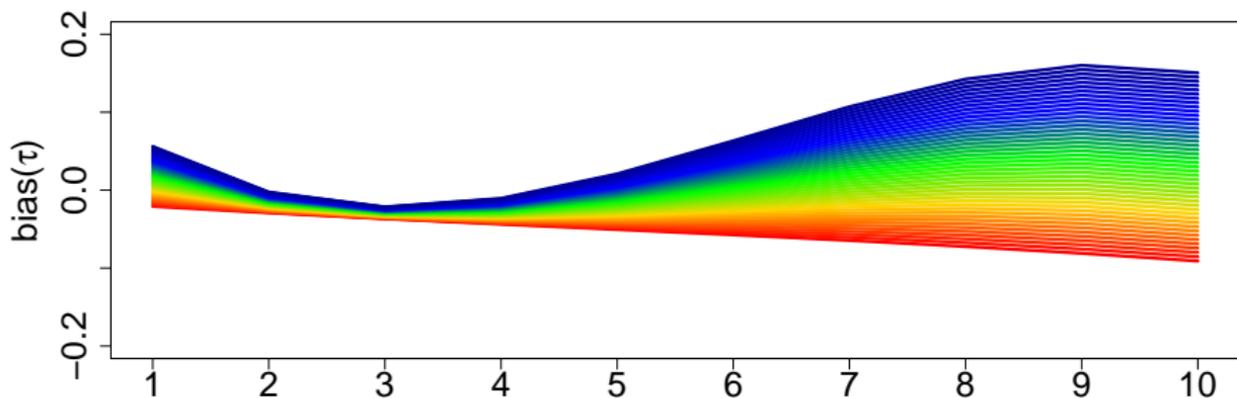
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tas, full-field initialisation,
red (early init, 1960) to blue (late init, 2004)

Drift ...

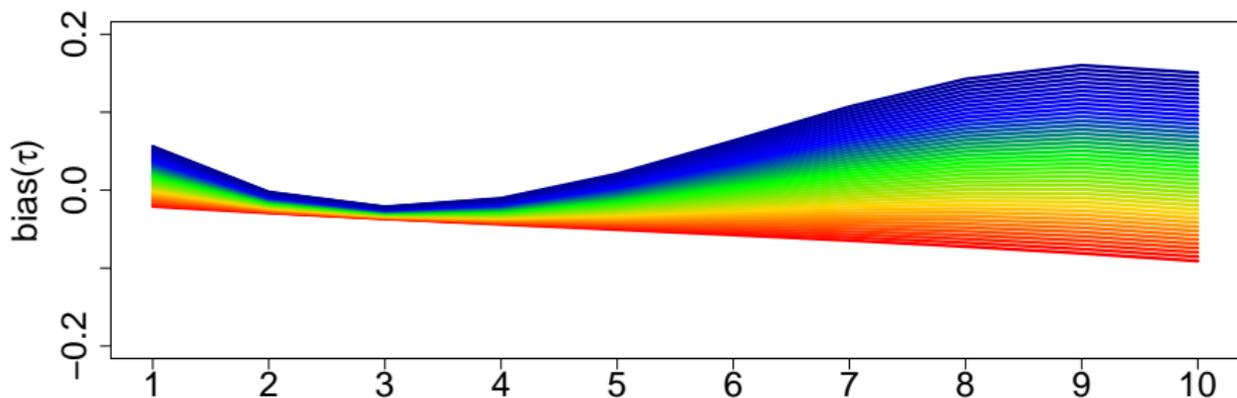
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tas, anomaly initialisation,
red (early init, 1960) to blue (late init, 2004)

Drift ...

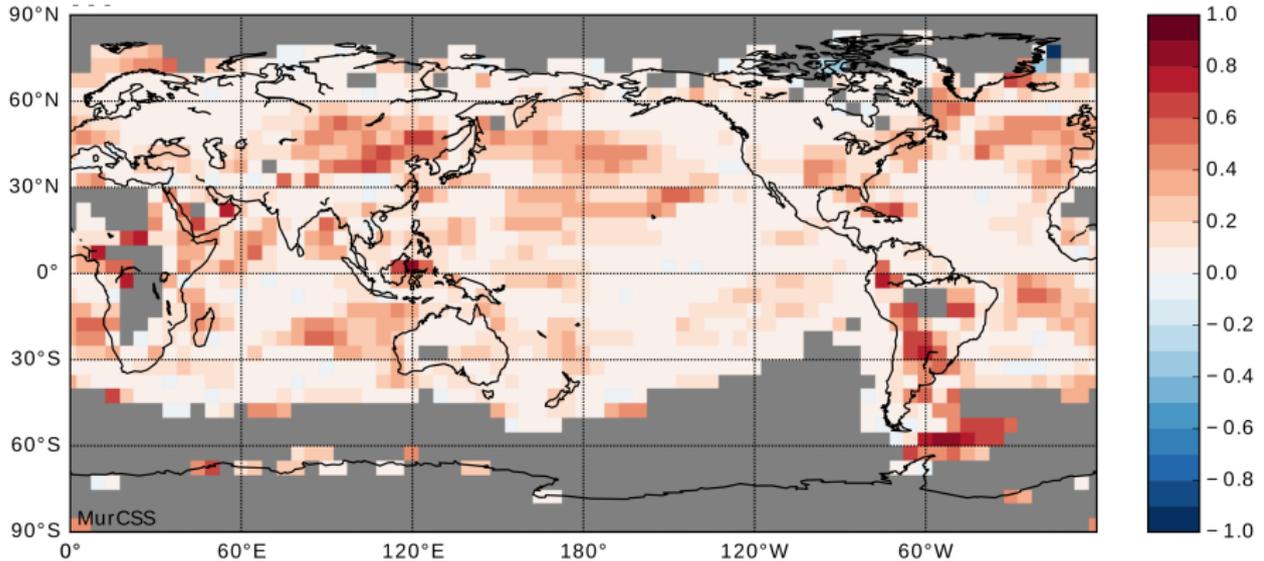
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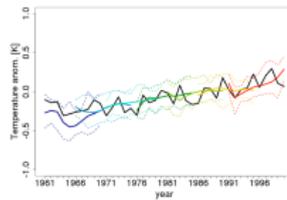
tas, anomaly initialisation,
red (early init, 1960) to blue (late init, 2004)

That seems complex! Does this help?

Parametric drift adjustment vs ICPO

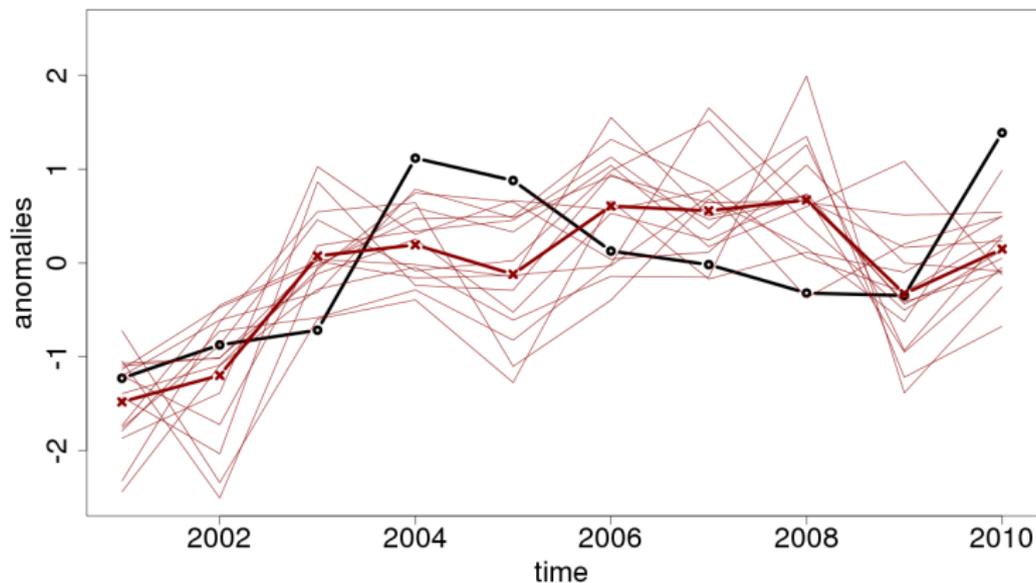


tas, full-field, MSESS, polynomial vs ICPO, yr2-5



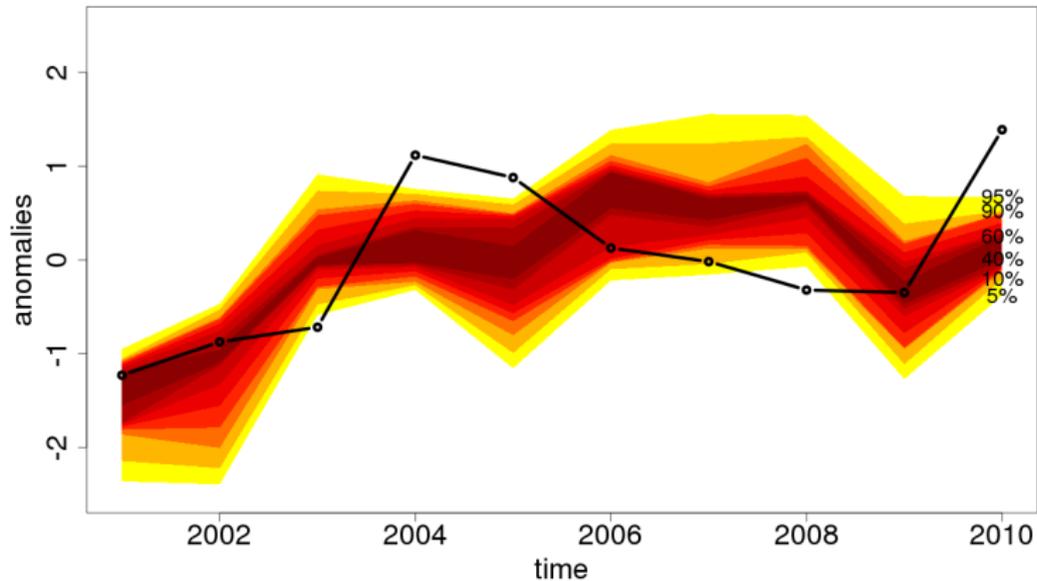
Re-calibration

Probabilistic forecast



all figures courtesy of Alexander Pasternack

Probabilistic forecast



all figures courtesy of Alexander Pasternack

Re-calibration method for decadal predictions

$$f_i(t, \tau) = \mu(t, \tau) + \epsilon_i(t, \tau)$$

⁶ $\mu(t, \tau)$: ensemble mean, $i = 1 \dots M$ member, t = init. year, τ = lead year

⁶e.g. Weigel et al. [2008]

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Re-calibrated ensemble

$$f_i^{Cal}(t, \tau) = \mu(t, \tau) + \epsilon_i(t, \tau)$$

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Re-calibration method for decadal predictions

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Re-calibrated ensemble

$$f_i^{\text{Cal}}(t, \tau) = \alpha(t, \tau) + \mu(t, \tau) + \epsilon_i(t, \tau)$$

1) α : bias and drift,

⁶e.g. Weigel et al. [2008]

Re-calibration method for decadal predictions

$$f_i(t, \tau) = \mu(t, \tau) + \epsilon_i(t, \tau)$$

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Re-calibrated ensemble

$$f_i^{Cal}(t, \tau) = \alpha(t, \tau) + \beta(t, \tau)\mu(t, \tau) + \epsilon_i(t, \tau)$$

1) α : bias and drift, 2) β : conditional bias,

⁶e.g. Weigel et al. [2008]

Re-calibration method for decadal predictions

$$f_i(t, \tau) = \mu(t, \tau) + \epsilon_i(t, \tau)$$

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Re-calibrated ensemble

$$f_i^{Cal}(t, \tau) = \alpha(t, \tau) + \beta(t, \tau)\mu(t, \tau) + \gamma(t, \tau)\epsilon_i(t, \tau)$$

1) α : bias and drift, 2) β : conditional bias, 3) γ : spread

⁶e.g. Weigel et al. [2008]

Re-calibration method for decadal predictions

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Re-calibrated ensemble

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1) α : bias and drift, 2) β : conditional bias, 3) γ : spread

find $\alpha(t, \tau)$, $\beta(t, \tau)$, $\gamma(t, \tau)$ such that ensemble is calibrated with maximum sharpness

⁶e.g. Weigel et al. [2008]

A model for α , β , and γ
a first go ^a:

$$\alpha(t, \tau) = (a_0 + a_1 t) + (a_2 + a_3 t)\tau + (a_4 + a_5 t)\tau^2 + (a_6 + a_7 t)\tau^3$$

^aPasternack et al. [2017]

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$$\gamma(t, \tau) = (c_0 + c_1t) + (c_2 + c_3t)\tau + (c_4 + c_5t)\tau^2 + (c_6 + c_7t)\tau^3$$

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$$\gamma(t, \tau) = (c_0 + c_1 t) + (c_2 + c_3 t)\tau + (c_4 + c_5 t)\tau^2 + (c_6 + c_7 t)\tau^3$$

Find parameters . . .

. . . by minimizing scores:

- CRPS [Gneiting et al. \[2005\]](#)
- ignorance score

[details](#)

^aPasternack et al. [2017]

A model for α , β , and γ
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$$\gamma(t, \tau) = (c_0 + c_1 t) + (c_2 + c_3 t)\tau + (c_4 + c_5 t)\tau^2 + (c_6 + c_7 t)\tau^3$$

Find parameters . . .

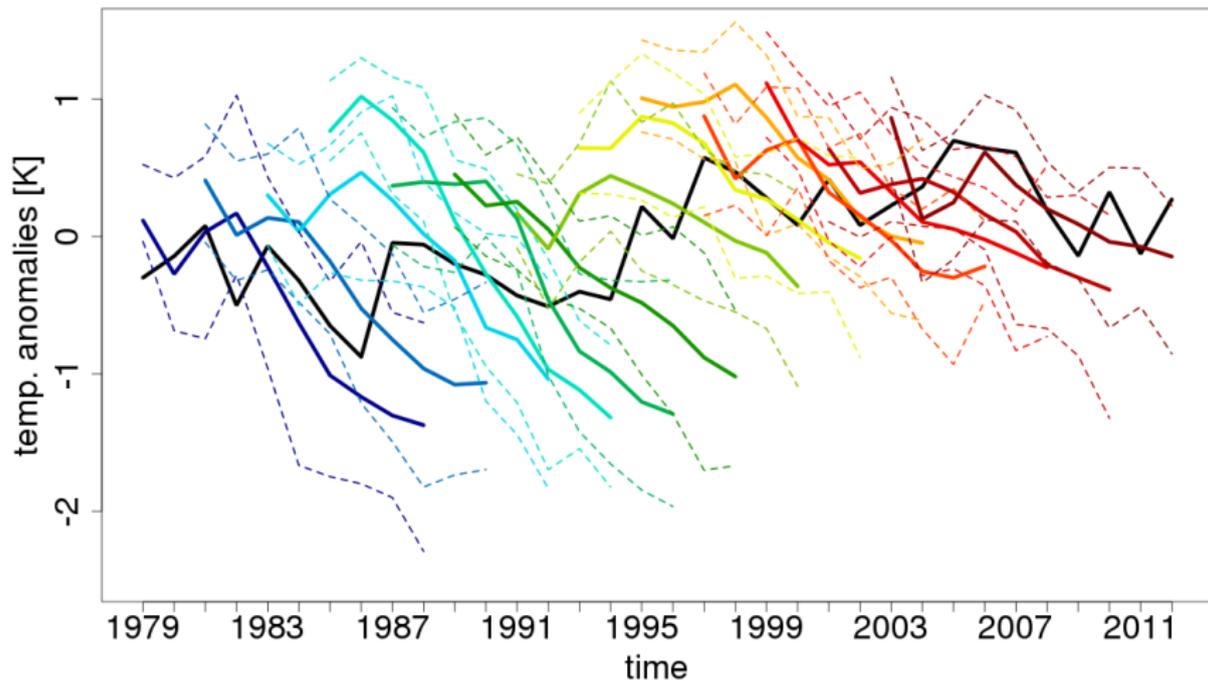
. . . by minimizing scores:

- CRPS Gneiting et al. [2005]
- ignorance score

details

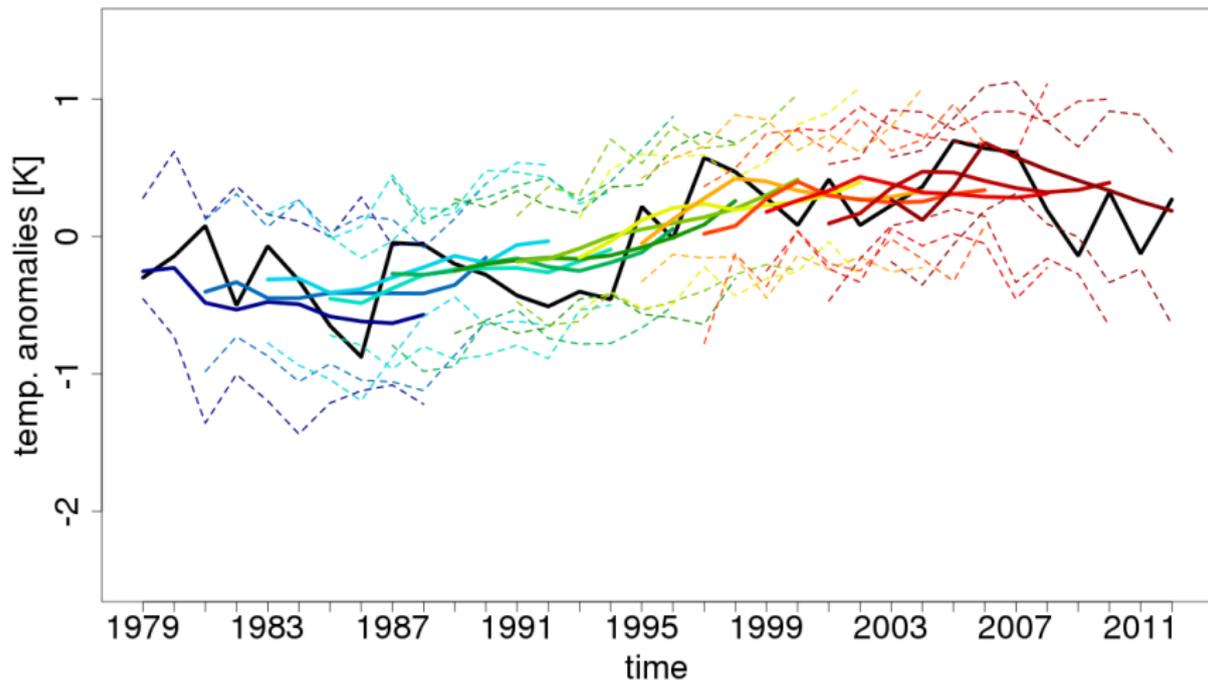
^aPasternack et al. [2017]

Re-calibration for MiKlip



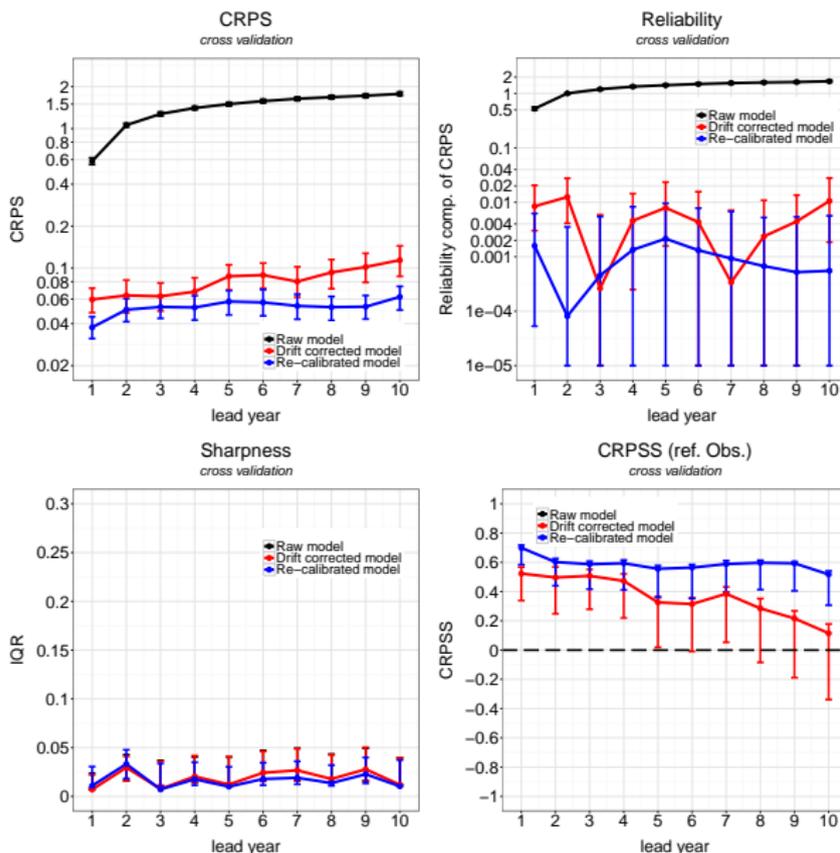
tas, global mean, full-field

Re-calibration for MiKlip



tas, global mean, full-field

Re-calibration for MiKlip – Verification

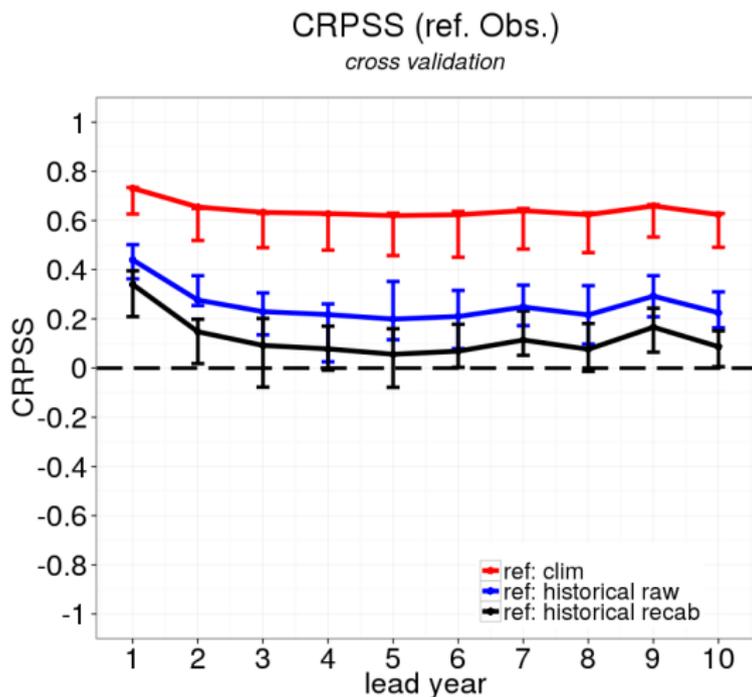


Re-calibration for MiKlip – Verification

Re-calibrating the historical simulations (reference):

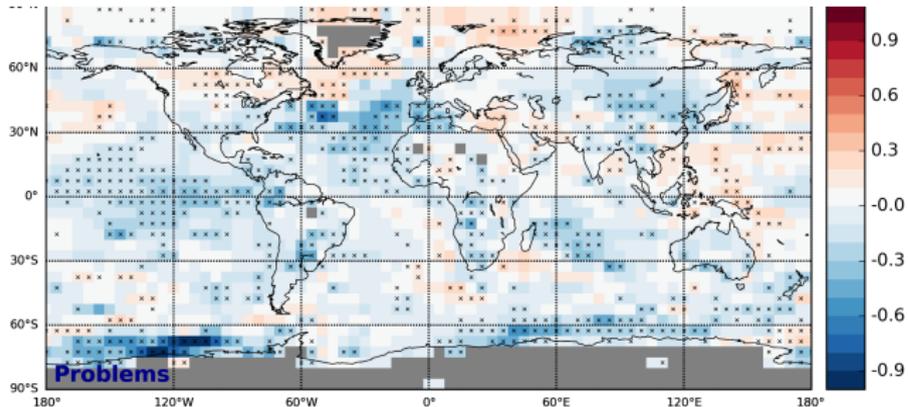
Re-calibration for MiKlip – Verification

Re-calibrating the historical simulations (reference):



Verifying grid-cells with CRPSS

mean surface temperature, lead-year 7-10, vs historical



PlotEngine 1.1.18 / 2017-02-01 23:08:28 (b324067@mksp3)

ICPO

param. drift correction
plus cond. bias
plus ensemble spread

$\alpha_{\text{ICPO}}(t, \tau)$

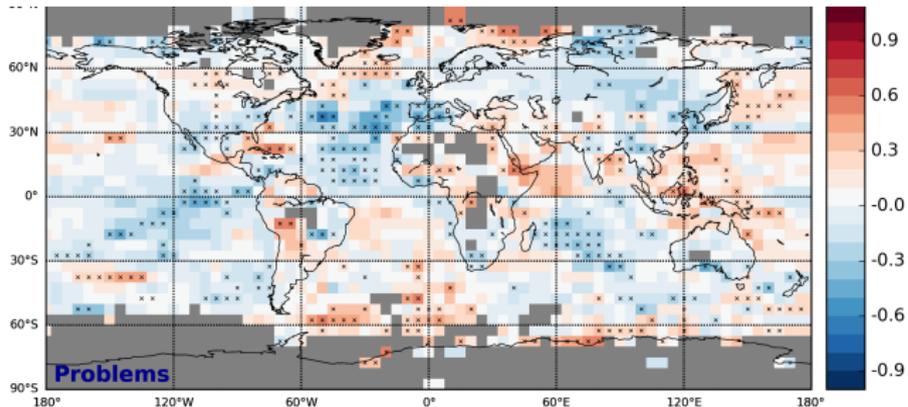
$\alpha(t, \tau)$

$\beta(t, \tau)$

$\gamma(t, \tau)$

Verifying grid-cells with CRPSS

mean surface temperature, lead-year 7-10, vs historical



PlotEngine 1.1.18 / 2017-02-01 22:20:39 (b324067@mltkp2)

ICPO

param. drift correction

plus cond. bias

plus ensemble spread

$\alpha_{\text{ICPO}}(t, \tau)$

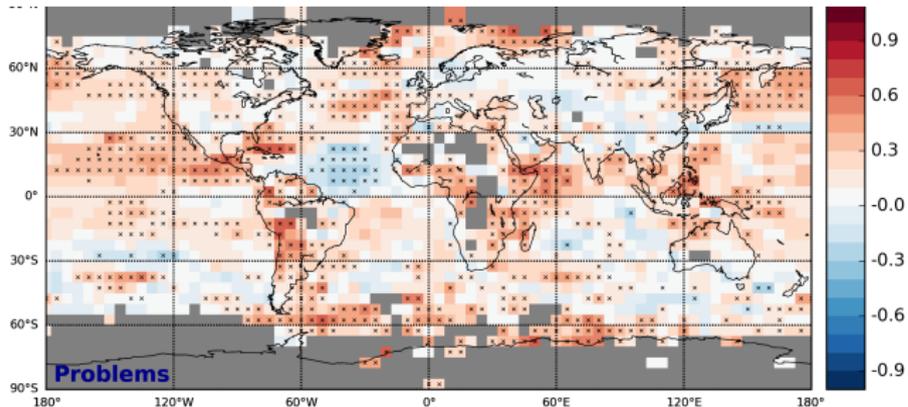
$\alpha(t, \tau)$

$\beta(t, \tau)$

$\gamma(t, \tau)$

Verifying grid-cells with CRPSS

mean surface temperature, lead-year 7-10, vs historical



PlotEngine 1.1.18 / 2017-02-02 19:19:33 (b324067@mlkpl)

ICPO

param. drift correction

plus cond. bias

plus ensemble spread

$\alpha_{\text{ICPO}}(t, \tau)$

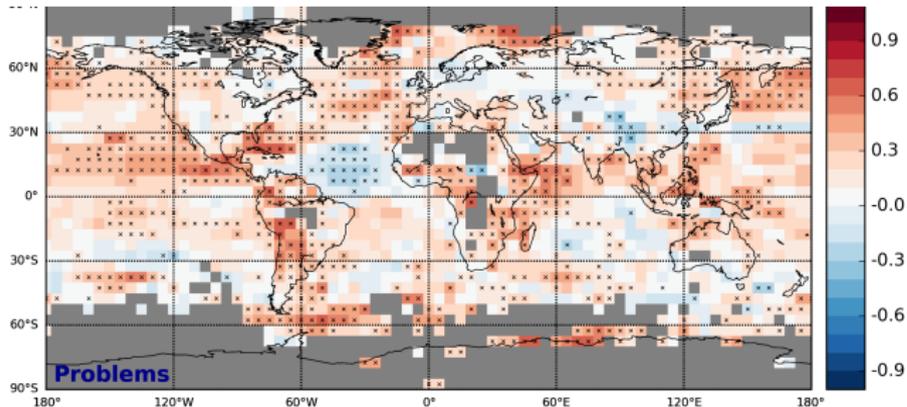
$\alpha(t, \tau)$

$\beta(t, \tau)$

$\gamma(t, \tau)$

Verifying grid-cells with CRPSS

mean surface temperature, lead-year 7-10, vs historical



PlotEngine 1.1.18 / 2017-02-01 23:05:25 (b324067@mlkpl)

ICPO

param. drift correction

plus cond. bias

plus ensemble spread

$$\alpha_{\text{ICPO}}(t, \tau)$$

$$\alpha(t, \tau)$$

$$\beta(t, \tau)$$

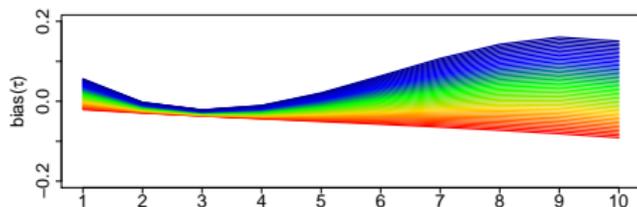
$$\gamma(t, \tau)$$

Summary

Verification of decadal predictions

- framework [Goddard et al. \[2013\]](#)
 - ensemble mean accuracy: MESS
 - ensemble spread: CRPS based σ_{ens}^2 vs MSE
 - consider: LESS
- (multi-)annual averages
- score corrections for small ensembles
- drift issue

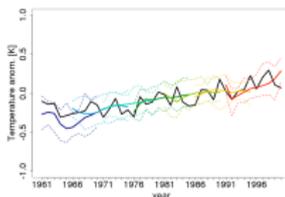
Summary



Drift adjustment

- $b = b(\tau, \mathbf{X}(t))$
- drift: full-field > anomaly initialisation
- parametric post-processing helps
- drift depending on climate not just on time [Fučkar et al. \[2014\]](#)

Summary



Re-calibration

- $f_i^{Cal} = \alpha(t, \tau) + \beta(t, \tau)\mu(t, \tau) + \gamma(t, \tau)\epsilon_i(t, \tau)$
- parametrics form for α, β, γ
- minimize CRPS/IGN to estimate parameters
- improves calibration, does not reduce sharpness (leave-10-yrs out cross validation)

Open issues

- grid-cell wise 'climate trend' estimation
- model selection
- parameter uncertainty

References

- G. J. Boer et al. The decadal climate prediction project (DCPP) contribution to CMIP6. *Geosci. Model Dev.*, 9:3751–77, 2016.
- C. A. T. Ferro et al. On the effect of ensemble size on the discrete and continuous ranked probability scores. *Meteor. Appl.*, 15:19 – 24, 2008.
- N. S. Fučkar et al. A posteriori adjustment of near-term climate predictions: Accounting for the drift dependence on the initial conditions. *Geophys. Res. Lett.*, 41(14):5200–5207, 2014.
- R. Gangstø et al. Methodological aspects of the validation of decadal predictions. *Clim. Res.*, 55: 181–200, 2013.
- T. Gneiting and A. E. Raftery. Strictly proper scoring rules, prediction, and estimation. *J. Amer. Statist. Assoc.*, 102(477):359–378, 2007.
- T. Gneiting et al. Calibrated probabilistic forecasting using ensemble model output statistics and minimum crps estimation. *Month. Weather Rev.*, 133:1098–1118, 2005.
- L. Goddard et al. A verification framework for interannual-to-decadal predictions experiments. *Climate Dynamics*, 40:245–272, 2013.
- C. Kadow et al. Evaluation of forecasts by accuracy and spread in the miklip decadal climate prediction system. *Met. Z.*, 01 2014.
- V. V. Kharin et al. Statistical adjustment of decadal predictions in a changing climate. *Geophys. Res. Lett.*, 39:L19705, 2012.
- T. Kruschke et al. Probabilistic evaluation of decadal predictions for northern hemisphere winter storms. *Meteorol. Z.*, 2015.
- G. A. Meehl et al. Decadal climate prediction: An update from the trenches. *Bull. Amer. Meteorol. Soc.*, 95(2):243–267, 2014.
- W. A. Müller et al. A debiased ranked probability skill score to evaluate probabilistic ensemble forecasts with small ensemble sizes. *J. Clim.*, 18(10): 1513–1523, 2005.
- A. Pasternack et al. Decadal forecast calibration – a parametric strategy accounting for drift, conditional bias and ensemble spread. *in preparation*, 2017.
- M. Pattantyús-Ábrahám et al. Bias and drift of the medium-range decadal climate prediction system (MiKlip) validated by european radiosonde data. *Meteorologische Zeitschrift*, pages 709–720, 2016.
- D. M. Smith, R. Eade, and H. Pohlmann. A comparison of full-field and anomaly initialization for seasonal to decadal climate prediction. *Climate Dynamics*, 41(11):3325–3338, 2013.
- A. P. Weigel, M. A. Liniger, and C. Appenzeller. Can multi-model combination really enhance the prediction skill of probabilistic ensemble forecasts? *Quart. J. Royal Meteor. Soc.*, 134(630): 241–260, 2008.